



Nombre: _____ Carné: _____

Fuerza Eléctrica, Campo eléctrico y Flujo eléctrico

$$F_e = \frac{k_e |q_1| |q_2|}{r^2} \quad \vec{F}_e = \frac{k_e |q_1| |q_2|}{r^2} \hat{r} \quad \hat{r} = \frac{\vec{r}}{|\vec{r}|} = \frac{\text{vector } r}{\text{magnitud del vector } r}$$

$$E = \frac{F}{q_0} = \frac{k_e |q|}{r^2} \quad \vec{E} = \frac{k_e |q|}{r^2} \hat{r} \quad \Phi_E = EA \cos \theta = \frac{Q_{\text{interior}}}{\epsilon_0} = 4\pi k_e q$$

$$\lambda = \frac{Q}{l} \quad \sigma = \frac{Q}{s} \quad \rho = \frac{Q}{V} \quad E = \frac{Q}{4\pi\epsilon_0 r^2} \quad E = \frac{\sigma}{2\epsilon_0}$$

Potencial Eléctrico y Capacitancia

$$\Delta EP = -W_{AB} = -qEd = k_e \frac{q_1 q_2}{r} = q_2 V_1 = q(V_B - V_A) \quad W = \frac{1}{2} mv^2 + |q|Ed$$

$$\Delta V = V_b - V_a = \frac{\Delta EP}{q} = \frac{k_e q}{r} = -E_x \Delta x \quad C = \frac{Q}{\Delta V} \quad C = \epsilon_0 \frac{A}{d} \quad C_{eq} = C_1 + C_2 + \dots$$

$$\frac{1}{C_{eq}} = \frac{1}{C_1} + \frac{1}{C_2} + \dots \quad U = \frac{1}{2} Q \Delta V = \frac{1}{2} C (\Delta V)^2 = \frac{Q^2}{2C} \quad P_{\text{promedio}} = \frac{\text{Energía Almacenada}}{\Delta t}$$

$$W = \frac{1}{2} Q \Delta V \quad C = \kappa \epsilon_0 \frac{A}{d}$$

Corriente y Resistencia

$$I = \frac{\Delta Q}{\Delta t} \quad I = \lim_{\Delta t \rightarrow 0} \frac{\Delta Q}{\Delta t} \quad Q = Ne \quad v_d = \frac{I}{nqA}$$

$$\Delta V = IR \quad R = \rho \frac{l}{A} \quad \rho = \rho_0 [1 + \alpha(T - T_0)] \quad R = R_0 [1 + \alpha(T - T_0)]$$

$$P = I \Delta V = I^2 R = \frac{(\Delta V)^2}{R} \quad P = I \Delta V - I^2 R$$

Circuito de Corriente Directa

$$\varepsilon = IR + Ir \quad R_{Eq} = R_1 + R_2 + \dots \quad \frac{1}{R_{eq}} = \frac{1}{R_1} + \frac{1}{R_2} + \dots$$

$$i_{\text{total}} = i_1 + i_2 \quad \sum \Delta V = \varepsilon + i_1 R_1 + i_3 R_2 + \dots = 0$$

$$q = Q(1 - e^{-t/RC}) \quad \tau = RC \quad q = Qe^{-t/RC} \quad i = Ie^{-t/RC}$$



Magnetismo

$$\begin{aligned}
 F &= qvB \sin \theta & \vec{F} &= q\vec{v} \times \vec{B} & F &= BIl \sin \theta & \vec{F} &= I\vec{l} \times \vec{B} \\
 \tau &= BIAN \sin \theta & \mu &= IAN & qB &= \frac{mv}{r} & F &= qE + q\vec{v} \times \vec{B} \\
 \phi &= BA \cos \theta & v &= \frac{E}{B} = \sqrt{\frac{2eV}{m}} & \tau &= \vec{\mu} \times \vec{B} & U &= -\vec{\mu} \cdot \vec{B} - \mu B \cos \phi \\
 \omega &= 2\pi f & v &= \omega r & T &= \frac{1}{f} & nq &= \frac{J_x B_y}{E_z} \quad J = \frac{I}{A} \\
 \vec{B} &= \frac{\mu_0}{4\pi} * \frac{q\vec{v} \times \hat{r}}{r^2} & & & & & |B| &= \frac{\mu_0}{4\pi} * \frac{qv \sin \phi}{r^2} \\
 d\vec{B} &= \frac{\mu_0}{4\pi} * \frac{Id\vec{l} \times \hat{r}}{r^2} = \frac{\mu_0}{4\pi} * \frac{Id\vec{l} \sin \phi}{r^2} & & & & & \vec{B} &= \frac{\mu_0}{4\pi} * \int \frac{Id\vec{l} \times \hat{r}}{r^2} \\
 B &= \frac{\mu_0 I}{2\pi r} & & & & & B_x &= \frac{N\mu_0 I a^2}{2(x^2 + a^2)^{3/2}} \\
 \frac{F}{L} &= \frac{\mu_0 I_1 I_2}{2\pi r} & & & & & B_x &= \frac{N\mu_0 I}{2a} \\
 B &= N \frac{\mu_0 I}{2R} & & & & & B &= \frac{\mu_0 I}{2\pi} * \frac{r}{R^2} \\
 B &= \mu_0 n I & & & & & B &= \frac{N\mu_0 I}{2\pi r} \\
 n &= \frac{N}{l} & & & & & \oint B dl &= \mu_0 I_{encerrada}
 \end{aligned}$$

Inducción electromagnética

$$\begin{aligned}
 d\Phi_B &= \vec{B} d\vec{A} & \Phi_B &= BA \cos \theta \\
 \varepsilon &= -N \frac{\Delta\Phi_B}{\Delta t} = -N \frac{d\Phi_B}{dt} = Blv & \varepsilon_{ce} &= \frac{2\varepsilon_{m\acute{a}x}}{\pi} \\
 \varepsilon &= NBA\omega \sin \omega t & E &= \frac{1}{2\pi r} \left| \frac{d\Phi_B}{dt} \right| \\
 \varepsilon_{m\acute{a}x} &= NBA\omega & \oint E d\vec{l} &= -\frac{d\Phi_B}{dt}
 \end{aligned}$$



$$I_D = \epsilon \frac{d\Phi_E}{dt}$$

$$\varepsilon = \oint (\vec{v} \times \vec{B}) d\vec{l}$$

$$I = \frac{Blv}{R}$$

$$L = \frac{-\varepsilon \Delta t}{\Delta I} = \frac{N \Delta \Phi_B}{\Delta I} = \frac{\mu_0 N^2 A}{l} = \mu_0 n^2 V$$

$$\varepsilon_2 = -M \frac{di_1}{dt}$$

$$\varepsilon_1 = -M \frac{di_2}{dt}$$

$$M = \frac{N_2 \Phi_{B_2}}{i_1} = \frac{N_1 \Phi_{B_1}}{i_2}$$

$$\frac{di}{dt} = \frac{\varepsilon - iR}{L}$$

$$i_0 = \frac{\varepsilon}{R}$$

$$\tau = \frac{L}{R}$$

$$i(t) = \frac{\varepsilon}{R} (1 - e^{-\tau/t})$$

$$\frac{di}{dt} = \frac{\varepsilon}{L} e^{-(R/L)t}$$

$$i(t) = i_0 e^{-(R/L)t}$$

$$U = L \int_0^I i dt = \frac{1}{2} LI^2$$

$$u = \frac{B^2}{2\mu_0} = \frac{\mu_0 N^2 A I^2}{4\pi r}$$

$$u = \frac{B^2}{2\mu}$$

Circuitos L-C y L-R-C

$$x = A \cos(\omega t + \phi)$$

$$q = Q \cos(\omega t + \phi)$$

$$\omega = \sqrt{\frac{1}{LC}}$$

$$I = -\omega Q \sin(\omega t + \phi)$$

$$U_{total} = \frac{1}{2} LI^2 + \frac{q^2}{2C} + \frac{Q_{m\acute{a}x}^2}{2C}$$

$$i = \pm \omega \sqrt{Q^2 - q^2}$$

$$q = A e^{-(R/2L)t} \cos\left(\sqrt{\frac{1}{LC} - \frac{R^2}{4L^2}} t + \phi\right)$$

$$\omega' = \sqrt{\frac{1}{LC} - \frac{R^2}{4L^2}}$$

Circuitos de corriente alterna

$$V = V_{m\acute{a}x} \cos \omega t$$

$$I = I_{m\acute{a}x} \cos \omega t$$

$$I_{(vmr)} = \frac{2}{\pi} I \approx 0.637 I$$

$$i_{(rms)} = \frac{I_{m\acute{a}x}}{\sqrt{2}}$$

$$V_{(rms)} = \frac{V_{m\acute{a}x}}{\sqrt{2}}$$

$$P_{prom} = I_{rms}^2 R$$

$$P = V_{rms} I_{rms}$$

$$V_{rms} = I_{rms} R$$

$$v_R = V_{m\acute{a}x} \cos \omega t = V_r \cos \omega t = IR \cos \omega t$$

$$q = \frac{I}{\omega} \sin \omega t$$

$$v_C = \frac{I}{\omega C} \cos\left(\omega t - \frac{\pi}{2}\right)$$

$$X_C = \frac{1}{\omega C} = \frac{1}{2\pi f C}$$

$$\varepsilon = IL\omega \cos\left(\omega t + \frac{\pi}{2}\right)$$

$$X_L = 2\pi f L$$

$$V_L = I X_L$$

$$V_C = I X_C$$



$$Z = \sqrt{R^2 + (X_L - X_C)^2} \quad V = IZ \quad \tan \phi = \frac{\omega L - \frac{1}{\omega C}}{R} \quad V_{rms} = I_{rms}Z = \frac{I_{max}Z}{\sqrt{2}}$$

$$P = \frac{1}{2}VI \cos \phi = V_{rms}I_{rms} \cos \phi \quad \phi = \frac{R}{Z}$$

Resonancia, Transformadores y Fasores

$$f_0 = \frac{1}{2\pi\sqrt{LC}} \quad \frac{V_1}{V_2} = \frac{N_1}{N_2} = \frac{I_1}{I_2} \quad P_E = I_1V_1 \quad P_S = I_2V_2$$

$$X_L = j\omega L \quad Z = R + jX_L \quad V = V_{max} \sin(\omega t + \phi)$$

$$V = (V_{max}, \phi) \quad \alpha \times \beta = \alpha + \beta \quad \frac{\alpha}{\beta} = \alpha - \beta$$

$$r = a + bj \quad |r| = \sqrt{a^2 + (bj)^2} \quad \tan \theta = \frac{a}{bj} \quad r = (|r|, \theta)$$

$$X_C = -j\left(\frac{1}{\omega C}\right) \quad Z = R - X_C \quad j = \sqrt{-1}$$

Constantes

Permeabilidad en el espacio libre

$$\mu_0 = 4\pi \times 10^{-7} T \cdot m/A$$

Relación entre Tesla y Gauss

$$1T = 10^4 G$$

Electrón-volt

$$1eV = 1.60 \times 10^{-19} C \cdot V = 1.60 \times 10^{-19} J$$

Constante de permitividad

$$\epsilon_0 = 8.85 \times 10^{-12} \frac{C^2}{N \cdot m^2}$$

Constantes

$$k_e = 8.9875 \times 10^9 \frac{Nm^2}{C^2}$$

Kilowatt-hora

$$3.60 \times 10^6 J$$

Tabla 1 Carga y masa de electrón, protón y neutrón

Partícula	Carga (C)	Masa (kg)
Electrón	-1.60×10^{-19}	9.11×10^{-31}
Protón	$+1.60 \times 10^{-19}$	1.67×10^{-27}
Neutrón	0	1.67×10^{-27}



Constantes dieléctricas y rigideces dieléctricas de varios materiales a temperatura ambiente

Material	Constante dieléctrica κ	Rigidez dieléctrica (V/m)
Aire	1.000 59	3×10^6
Baquelita [®]	4.9	24×10^6
Cuarzo fundido	3.78	8×10^6
Neopreno	6.7	12×10^6
Nylon	3.4	14×10^6
Papel	3.7	16×10^6
Poliestireno	2.56	24×10^6
Vidrio Pyrex [®]	5.6	14×10^6
Aceite de silicona	2.5	15×10^6
Titanato de estroncio	233	8×10^6
Teflón [®]	2.1	60×10^6
Vacío	1.000 00	—
Agua	80	—

Resistividades y coeficientes de temperatura de la resistividad para varios materiales (a 20 °C)

Material	Resistividad ($\Omega \cdot m$)	Coefficiente de temperatura de la resistividad [$(^{\circ}C)^{-1}$]
Plata	1.59×10^{-8}	3.8×10^{-3}
Cobre	1.7×10^{-8}	3.9×10^{-3}
Oro	2.44×10^{-8}	3.4×10^{-3}
Aluminio	2.82×10^{-8}	3.9×10^{-3}
Tungsteno	5.6×10^{-8}	4.5×10^{-3}
Hierro	10.0×10^{-8}	5.0×10^{-3}
Platino	11×10^{-8}	3.92×10^{-3}
Plomo	22×10^{-8}	3.9×10^{-3}
Nicromo ^a	150×10^{-8}	0.4×10^{-3}
Carbono	3.5×10^{-5}	-0.5×10^{-3}
Germanio	0.46	-48×10^{-3}
Silicio	640	-75×10^{-3}
Vidrio	$10^{10} - 10^{14}$	
Caucho duro	$\approx 10^{13}$	
Azufre	10^{15}	
Cuarzo (fundido)	75×10^{16}	

^aAleación de níquel-cromo de uso común en elementos calefactores.